

**Problem 1.** In each case, say whether or not the function is a polynomial.

(a)  $f(x) = x^2 + 5x^{-1}$ ;

(b)  $f(x) = x^3 + \sqrt{x}$ ;

(c)  $f(x) = \frac{1}{2}x^2 + x - \sqrt{2}$ .

**Problem 2.** In each case, identify the degree, the leading coefficient, and the constant coefficient.

(a)  $f(x) = x$ ;

(b)  $f(x) = 2x + x^3 - \sqrt{2} + 3x^2$ ;

(c)  $f(x) = x^2 + x + 1 + x + x^2 + x$ .

**Problem 3.** Let  $f(x) = x^3 - 19x + 30$ .

(a) Verify that  $f(2) = 0$ .

(b) Divide  $f(x)$  by  $x - 2$ .

(c) Find all roots of  $f(x)$ .

**Problem 4 (Extra Credit).** The locus of the equation  $x^2 + y^2 = 9$  is a circle of radius 3 centered at the origin. The line  $y = 2x$  intersects this circle in two points. Find these points. Justify your answer.